# Package: mixedMem (via r-universe)

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Type Package Title Tools for Discrete Multivariate Mixed Membership Models Version 1.2.0 Date 2016-04-4 Maintainer Y. Samuel Wang <ysamwang@uw.edu> Description Fits mixed membership models with discrete multivariate data (with or without repeated measures) following the general framework of Erosheva et al (2004). This package includes a Variational EM and MCMC estimation approaches. Currently supported data types are Bernoulli, multinomial and rank (Plackett-Luce). The extended GoM model with fixed stayers from Erosheva et al (2007) is now also supported. See Airoldi et al (2014) for other examples of mixed membership models. License GPL (>= 2) **Depends** R (>= 3.0.2) Imports Rcpp (>= 0.11.3), gtools, R.utils LazyData TRUE LinkingTo Rcpp (>= 0.11.3), RcppArmadillo, BH VignetteBuilder knitr Suggests knitr, xtable, RoxygenNote 5.0.1 Repository https://ysamwang.r-universe.dev RemoteUrl https://github.com/ysamwang/mixedmem RemoteRef HEAD RemoteSha d830b4de68027fee4ebf08a5fa8ed71e530e4553

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mixedMem-package Tools for fitting discrete multivariate mixed membership models

## Description

The mixedMem package contains tools for fitting and interpreting discrete multivariate mixed membership models following the general framework outlined in Erosheva et al 2004. In a mixed membership models, individuals can belong to multiple groups instead of only a single group (Airoldi et al 2014). This extension allows for a richer description of heterogeneous populations and has been applied in a wide variety of contexts including: text data (Blei et al 2003), genotype sequences (Pritchard et al 2000), ranked data (Gormley and Murphy 2009), and survey data (Erosheva et al 2007, Gross and Manrique-Vallier 2014).

#### Details

Mixed membership model objects can be created using the mixedMemModel constructor function. This function checks the internal consistency of the data/parameters and returns an object suitable for use by the mmVarFit function. The mmVarFit function is the main function in the package. It utilizes a variational EM algorithm to fit an approximate posterior distribution for the latent variables and select pseudo-MLE estimates for the global parameters. A step-by-step guide to using the package is detailed in the package vignette "Fitting Mixed Membership Models using mixedMem".

The package supports multivariate models (with or without repeated measurements) where each variable can be of a different type. Currently supported data types include: Bernoulli, rank (Plackett-Luce) and multinomial. Given a fixed number of sub-populations K, we assume the following generative model for each mixed membership model:

- For each individual i = 1,... Total:
  - Draw λ<sub>i</sub> from a Dirichlet(α). λ<sub>i</sub> is a vector of length K whose components indicates the degree of membership for individual i in each of the K sub-populations.
  - For each variable  $j = 1 \dots, J$ :
  - For each of replicate  $r = 1, ..., R_i$ :
  - For each ranking level  $n = 1..., N_{i,j,r}$ :
    - \* Draw  $Z_{i,j,r,n}$  from a multinomial(1,  $\lambda_i$ ). The latent sub-population indicator  $Z_{i,j,r,n}$  determines the sub-population which governs the response for observation  $X_{i,j,r,n}$ . This is sometimes referred to as the context vector because it determines the context from which the individual responds.
    - \* Draw  $X_{i,j,r,n}$  from the latent sub-population distribution parameterized by  $\theta_{j,Z_{i,j,r,n}}$ . The parameter  $\theta$  governs the observations for each sub-population. For example, if variable j is a multinomial or rank distribution with  $V_j$  categories/candidates, then  $\theta_{j,k}$  is a vector of length  $V_j$  which parameterizes the responses to variable j for sub-population k. Likewise, if variable j is a Bernoulli random variable, then  $\theta_{j,k}$  is a value which determines the probability of success.

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#### References

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Pritchard, Jonathan K.; Stephens, Matthew; Donnelly, Peter. 2000. Inference of Population Structure using Multilocus Genotype Data. Genetics 155.2: 945-959.

Gross, Justin; Manrique-Vallier, Daniel. 2014. A Mixed-membership Approach to the Assessment of Political Ideology from Survey Responses. In Airoldi, Edoardo M.; Blei, David; Erosheva, Elena A.; & Fienberg, Stephen E.. Handbook of Mixed Membership Models and Their Applications. CRC Press. Chicago

#### Examples

```
library(mixedMem)
data(ANES)
# Dimensions of the data set: 279 individuals with 19 responses each
dim(ANES)
# The 19 variables and their categories
# The specific statements for each variable can be found using help(ANES)
# Variables titled EQ are about Equality
# Variables titled IND are about Econonic Individualism
# Variables titled ENT are about Free Enterprise
colnames(ANES)
# Distribution of responses
table(unlist(ANES))
# Sample Size
Total <- 279
# Number of variables
J <- 19
# we only have one replicate for each of the variables
R_j <- rep(1, J)
# Nijr indicates the number of ranking levels for each variable.
# Since all our data is multinomial it should be an array of all 1s
Nijr <- array(1, dim = c(Total, J, max(Rj)))</pre>
# Number of sub-populations
K <- 3
# There are 3 choices for each of the variables ranging from 0 to 2.
Vj <- rep(3, J)
# we initialize alpha to .2
alpha <- rep(.2, K)
# All variables are multinomial
dist <- rep("multinomial", J)</pre>
# obs are the observed responses. it is a 4-d array indexed by i,j,r,n
\# note that obs ranges from 0 to 2 for each response
obs <- array(0, dim = c(Total, J, max(Rj), max(Nijr)))</pre>
obs[ , ,1,1] <- as.matrix(ANES)</pre>
# Initialize theta randomly with Dirichlet distributions
set.seed(123)
theta <- array(0, dim = c(J,K,max(Vj)))</pre>
for(j in 1:J)
{
    theta[j, , ] <- gtools::rdirichlet(K, rep(.8, Vj[j]))</pre>
}
# Create the mixedMemModel
# This object encodes the initialization points for the variational EM algorithim
```

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## ANES

ANES

Responses from 1983 American National Election Survey Pilot

#### Description

ANES contains political ideology survey data from the 1983 American National Election Survey Pilot. Respondents were read a value statement and asked to report their level of agreement: 'strongly agree', 'agree', 'can't decide', 'disagree', and strongly disagree'. The 279 complete responses to the 19 statements selected by Feldman (1988) and reanalyzed by Gross and Manrique-Vallier (2014) are included. 'Strongly disagree' and 'disagree' as well as 'strongly agree' and 'agree' have been collapsed into single categories. 0 indicates 'agree', 1 indicates 'can't decide', and 2 indicates 'disagree'. The statements have been grouped into 3 overarching themes as indicated in the variable names- Equality (EQ), Economic Individualism (IND), and Free Enterprise (ENT). Variable ID's from the original ANES questionnaire are included in parentheses. An example analysis of the data is included in the "Fitting Mixed Membership Models Using mixedMem" vignette.

#### Usage

data(ANES)

## Format

A data frame with 279 individuals and 19 variables:

- EQ1 If people were treated more equally in this country, we would have many fewer problems (V832169)
- EQ2 We should give up on the goal of equality, since people are so different to begin with (V832172)
- EQ3 Our society should do whatever is necessary to make sure that everyone has an equal opportunity to succeed (V832175)
- EQ4 Some people are just better cut out than others for important positions in society (V832178)
- EQ5 Some people are better at running things and should be allowed to do so (V832250)
- EQ6 All kinds of people should have an equal say in running this country, not just those who are successful (V832253)
- EQ7 One of the big problems in this country is that we don't give everyone an equal chance (V832256)

- **IND1** Any person who is willing to work hard has a good chance of succeeding (V832170)
- **IND2** Hard work offers little guarantee of success (V832173)
- **IND3** Most people who don't get ahead should not blame the system; they really have only themselves to blame (V832176)
- **IND4** Even if people are ambitious, they often cannot succeed (V832251)
- IND5 If people work hard, they almost always get what they want (V832254)
- IND6 Even if people try hard, they often cannot reach their goals (V832257)
- **ENT1** The less government gets involved with business and the economy, the better off this country will be (V832171)
- **ENT2** There are many goods and services that would never be available to ordinary people without governmental intervention (V832174)
- **ENT3** There should be no government interference with business and trade (V832177)
- ENT4 Putting government regulations on business does not endanger personal freedom (V832252)
- ENT5 Government intervention leads to too much red tape and too many problems (V832255)
- **ENT6** Contrary to what some people think, a free enterprise system is not necessary for our form of government to survive (V832258)

#### References

Feldman, Stanley. "Structure and consistency in public opinion: The role of core beliefs and values." American Journal of Political Science (1988): 416-440.

Gross, J.H. and Manrique-Vallier, D. "A Mixed-Membership Approach to the Assessment of Political Ideology from Survey Responses." in Airoldi, E. M., Blei, D. M., Erosheva, E. A., and Fienberg, S. E. Handbook of Mixed Membership Models and Its Applications. Chapman & Hall/CRC, 2014

National Election Studies, 1983 Pilot Election Study. Ann Arbor, MI: University of Michigan, Center for Political Studies, 1999

computeAIC

Compute the approximate AIC

#### Description

computeAIC computes the approximate AIC of a given mixedMemModelVI, where the lower bound on the log-likelihood (also called ELBO) is used instead of the intractable true log-likelihood.

#### Usage

```
computeAIC(model)
```

#### Arguments

model

the mixedMemModelVI object for which the AIC will be calculated.

#### computeBIC

#### Details

AIC = -2ELBO + 2 \* p

where p is the number of estimated parameters.

#### Value

computeAIC returns the approximate AIC value, a real number.

computeBIC

*Compute the approximate BIC* 

#### Description

computeBIC computes the approximate BIC of a given mixedMemModelVI, where the lower bound on the log-likelihood (also called ELBO) is used instead of the intractable true log-likelihood.

#### Usage

computeBIC(model)

## Arguments

model the mixedMemModel object for which the BIC will be calculated.

## Details

 $BIC = -2ELBO + p \log(Total)$ 

where p is the number of estimated parameters and Total is the number of individuals in the sample.

This BIC model selection criteria is used in Erosheva et al (2007). The number of estimated parameters P includes the parameters  $\theta$  and  $\alpha$ , but omits the variational parameters  $\phi$  and  $\delta$ .

## Value

computeBIC returns the approximate BIC value, a real number.

#### References

Erosheva, E. A., Fienberg, S. E., & Joutard, C. (2007). Describing disability through individuallevel mixture models for multivariate binary data. The annals of applied statistics, 1(2), 346. computeELB0

## Description

computeELBO computes the variational lower bound on the log-likelihood, also called the ELBO, for a mixed membership model.

#### Usage

computeELBO(model)

#### Arguments

model

a mixedMemModelVarInf object created by the mixedMemModelVarInf constructor.

## Details

The lower bound (ELBO) is the objective function in the variational EM algorithm. It is a function of the latent variables ( $\phi$  and  $\delta$ ) and the parameters ( $\alpha$  and  $\theta$ ) that be derived from Jensen's inequality:

 $E_Q \log[p(X, Z, \Lambda)] - E_Q \log[Q(Z, \Lambda | \phi, \delta)] \le \log P(obs | \alpha, \theta)$ 

## Value

computeELBO returns the lower bound on the log-likelihood, a real number.

ct\_hagdu

Responses Chlamydia trachomatis test data

## Description

ct\_hagdu contains

#### Usage

data(ct\_hagdu)

#### ct\_hagdu

#### Format

A data frame with 279 individuals and 19 variables:

- EQ1 If people were treated more equally in this country, we would have many fewer problems (V832169)
- EQ2 We should give up on the goal of equality, since people are so different to begin with (V832172)
- EQ3 Our society should do whatever is necessary to make sure that everyone has an equal opportunity to succeed (V832175)
- EQ4 Some people are just better cut out than others for important positions in society (V832178)
- EQ5 Some people are better at running things and should be allowed to do so (V832250)
- **EQ6** All kinds of people should have an equal say in running this country, not just those who are successful (V832253)
- EQ7 One of the big problems in this country is that we don't give everyone an equal chance (V832256)
- IND1 Any person who is willing to work hard has a good chance of succeeding (V832170)
- **IND2** Hard work offers little guarantee of success (V832173)
- **IND3** Most people who don't get ahead should not blame the system; they really have only themselves to blame (V832176)
- **IND4** Even if people are ambitious, they often cannot succeed (V832251)
- IND5 If people work hard, they almost always get what they want (V832254)
- **IND6** Even if people try hard, they often cannot reach their goals (V832257)
- ENT1 The less government gets involved with business and the economy, the better off this country will be (V832171)
- **ENT2** There are many goods and services that would never be available to ordinary people without governmental intervention (V832174)
- ENT3 There should be no government interference with business and trade (V832177)
- ENT4 Putting government regulations on business does not endanger personal freedom (V832252)
- ENT5 Government intervention leads to too much red tape and too many problems (V832255)
- **ENT6** Contrary to what some people think, a free enterprise system is not necessary for our form of government to survive (V832258)

## References

Feldman, Stanley. "Structure and consistency in public opinion: The role of core beliefs and values." American Journal of Political Science (1988): 416-440.

Gross, J.H. and Manrique-Vallier, D. "A Mixed-Membership Approach to the Assessment of Political Ideology from Survey Responses." in Airoldi, E. M., Blei, D. M., Erosheva, E. A., and Fienberg, S. E. Handbook of Mixed Membership Models and Its Applications. Chapman & Hall/CRC, 2014

National Election Studies, 1983 Pilot Election Study. Ann Arbor, MI: University of Michigan, Center for Political Studies, 1999

```
entropyPlot
```

## Description

entropyPlot plots a histogram of the entropy of each individuals estimated mixed membership. The entropy is is roughly the number of profiles needed to model each individual (Gormley and Murphy 2014; White et al 2012).

#### Usage

## Arguments

model	the mixedMemModel the model to be plotted
col	the color of the bars
main	the main title
xlab	the label for the x-axis

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## Description

Mixed Membership models are invariant to permutations of the sub-population labels; swapping the names of each sub-population yields an equivalent model. The ordering of the labels in a fitted model is often dependent on the initialization points. The function findLabels selects a permutation of the sub-population labels that best matches a given comparison model by minimizing squared differences between the  $\theta$  arrays.

## Usage

```
findLabels(model, comparison, exhaustive = FALSE)
```

#### Arguments

model	the fitted mixedMemModelMCMC or mixedMemModelVarInf object.
comparison	an array of the same dimensions as model\$theta which contains the subpopula-
	tion parameters from another model. findLabels will return a permutation of
	the labels of model which match to comparison most closely.
exhaustive	a boolean for whether an exhaustive search should be performed. If false, a
	greedy algorithim is used instead.

## Details

 $Loss = \sum_{j} \sum_{k} [\sum_{v} (\hat{\theta}_{k,v} - \theta_{k,v})^2]$ 

If K, number of sub-populations, is small, the method searches through all K! permutations of the sub-population labels and select the permutation which minimizes the loss. If K is large, a greedy algorithm can be used instead. This algorithm selects the best match for each fitted sub-population starting with the group with the largest fitted relative frequency.

## Value

findLabels returns a list with two objects: perm and loss. perm is the optimal permutation of the labels with respect to the squared error loss. loss is the calculated value of the weighted squared error loss (shown above) for the optimal permutation.

## See Also

permuteLabels

#### Examples

```
## Not run:
# See mixedMemModelMCMC or mixedMemModelVarInf documentation for how to generate data and instantiate objects
# After the data as been generated, we initialize the array of sub-population parameters (theta)
# according to a permutation of the true labeling
set.seed(123)
perm <- sample.int(K, size = K, replace = FALSE)</pre>
theta.perm <- theta_truth[,perm,]</pre>
test_model <- mixedMemModelVarInf(Total = Total, J = J,Rj = Rj, Nijr= Nijr,</pre>
K = K, Vj = Vj, dist = dist, obs = obs, alpha = alpha, theta = theta.perm)
out <- mmVIFit(test_model)</pre>
opt.perm <- findLabels(out, theta_truth)</pre>
opt.perm
# produce mixedMemModel object with sub-population labels permuted to best match
# the comparison model
out <- permuteLabels(out, opt.perm$perm)</pre>
## End(Not run)
```

getPosteriorEstimates *Mixed Membership Post-Processing for MCMC method* getPosteriorEstimates

#### Description

Mixed Membership Post-Processing for MCMC method getPosteriorEstimates

#### Usage

```
getPosteriorEstimates(model, fileNames = c("theta.csv", "alpha.csv",
    "ksi.csv", "lambda.csv", "z.csv", "p.csv", "rho.csv"), whichWrite = c(1, 1,
    1, 0, 0, 1, 0))
```

#### Arguments

model	the fitted mixedMemModelMCMC object.
fileNames	a vector of strings containing the file paths for the MCMC output The string should be of length 7 for theta, alpha, ksi, lambda, Z, P and StayerStatus. If the particular parameter was not recorded, insert an empty string ("") as a place-holder
whichWrite	a vector of length 7 indicating which files to be read. 1 indicates read, 0 indicates skip

hellingerDistances	Mixed membership models post-processing
--------------------	---

#### Description

hellingerDistances computes hellinger distances between each sub-population for each variable

## Usage

```
hellingerDistances(model)
```

#### Arguments

model the mixedMemModelVI object that will be plotted.

mixedMemModelMCMC Constructor for a Mixed Membership Model object which can be fit through MCMC

## Description

Constructor for a mixedMemModelMCMC object which can be fit using MCMC in the mixedMem package.

## Usage

```
mixedMemModelMCMC(Total, J, dist, Rj = rep(1, J), Vj, obs, K, theta, alpha0,
ksi, lambda = NULL, Z = NULL, tau, beta, gamma, extended = 0,
P = NULL, S = NULL, fixedObs = NULL)
```

## Arguments

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Total	the number of individuals in the sample.
J	the number of variables observed on each individual.
dist	a vector of length J specifying variable types. Options are "bernoulli" or "multi- nomial" corresponing to the distributions of the observed variables.
Rj	a vector of length J specifying the number of repeated measurements for each variable.
Vj	a vector of length J specifying the number of possible responses for each variable. For a Bernoulli variable $\forall j[j] = 1$ .
obs	an array with dimensions (Total,J,max(Rj)) corresponding to the observed data. For Bernoulli random variables, the data consist of 0/1's. For multinomial the data consist of integers $0,1,\ldots,(Vj[j]-1)$ .
К	the number of sub-populations.
theta	an array with dimensions $(J,K,max(Vj))$ which governs the variable distribu- tions. The parameter theta[j,k,] governs the distribution of variable J for a complete member of sub-population k. For instance, if variable j is a Bernoulli variable, theta[j,k,1] is the probability of success; if variable j is a multinomial variable, theta[j,k, 1:Vj[j]] is the probability for each of the Vj[j] categories. Since the dimension of the relevant parameters can differ across variables, any unused elements of the array should be set to 0, while all other elements should be positive.
ksi	a vector which lies in the K-1 simplex which represents the relative frequency of each sub-population
lambda	a matrix with dimensions (Total, K) which represent the partial membership for individual i in group ${\bf k}$
Z	an array with dimensions (Total, J, max (Rj)) which represents the sub-population according to which individual i responded to the r repitition of variable j
tau	an array of dimension (J, K, max(2, max(Vj))) which holds the prior parameters for each of the theta parameters. Note that for Bernoulli variables, even though Vj = 1, both parameters of the beta must be specified so we still require 2 values
beta	shape parameter for prior for alpha
gamma	scale parameter for prior for alpha
extended	1 indicates the extended GoM model is being used; 0 indicates the normal mixed membership model without fixed stayers
Ρ	vector of length S + 1 which lies in S dimensional simplex indicating the proportion of individuals in the fixed groups and GoM compartment. The first S elements correspond to the stayer classes, while the S + 1 element indicates the proportion of individuals in GoM compartment
S	integer indicating the number of fixed stayer classes if extended GoM is used.
fixedObs	an array with dimensions (S, J, $max(Rj)$ ) corresonding to the observed responses for a fixed group in the extended GoM model from Erosheva et al (2007).
alpha	a scalar representing the sum of the dirichlet membership parameters

#### Details

The function returns an object of mixedMemModelMCMC class. This object contains dimensions of the model, the observed data, and the model parameters. Once a mixedMemModel object is created, the specified model can be fit for the data using the mmMCMCFit function. If the inputs are inconsistent (ie if dimensions do not match, or if observations and distribution types are not compatible, mixedMemModelMCMC will throw an error. Supported data types include Bernoulli and Multinomial (Note that rank data is not supported in the MCMC method). The MCMC method is capable of also estimating the extended GoM model which allows for a fixed number of "stayers". See Erosheva et al (2007) for a detailed description of the extended GoM Model. For additional details on usage, and model assumptions, see the corresponding vignette "Fitting Mixed Membership Models Using mixedMem".

## Value

returns an object of class mixedMemModelMCMC.

mixedMemModelVarInf	Constructor for a Mixed Membership Model object which can be fit
	using variational inference

#### Description

Constructor for a mixedMemModelVI object which can be used be fit using variational inference in the mixedMem package.

#### Usage

```
mixedMemModelVarInf(Total, J, Rj = rep(1, J), Nijr = array(1, dim = c(Total,
    J, max(Rj))), K, Vj, alpha, theta, phi = NULL, delta = NULL, dist, obs)
```

#### Arguments

Total	the number of individuals in the sample.
J	the number of variables observed on each individual.
Rj	a vector of length J specifying the number of repeated measurements for each variable.
Nijr	an array with dimension (Total, J, max(Rj)) indicating the number of ranking levels for each variable and each replication. For multinomial and Bernoulli variables, Nijr[i,j,r] = 1. For rank variables, Nijr[i,j,r] indicates the number of alternatives ranked.
К	the number of sub-populations.
Vj	a vector of length J specifying the number of possible responses for each variable. For a Bernoulli variable $Vj[j] = 1$ .
alpha	a vector of length K which is the parameter for Dirichlet membership distribu- tion.

#### 14

theta	an array with dimensions (J,K,max(Vj)) which governs the variable distribu- tions. The parameter theta[j,k,] governs the distribution of variable J for a complete member of sub-population k. For instance, if variable j is a Bernoulli variable, theta[j,k,1] is the probability of success; if variable j is a multinomial variable, theta[j,k, 1:Vj[j]] is the probability for each of the Vj[j] categories; if variable j is a rank variable, theta[j,k, 1:Vj[j]] are the support parameters for each of the Vj[j] possible categories. Since the dimension of the relevant param- eters can differ across variables, any unused elements of the array should be set to 0, while all other elements should be positive.
phi	an array with dimensions (Total,K) which specifies the variational parameters for the membership vectors, $\lambda$ . The default group membership initialization is uniform across all groups (phi[i,k] = 1/K for all k). The default initialization is highly recommended.
delta	an array with dimensions (Total,J,max(Rj), max(Nijr), K) which specifies the variational parameters for the context vectors Z. The default initialization is uniform across all sub-populations (delta[i, j, r, n, k] = $1/K$ for all k).
dist	a vector of length J specifying variable types. Options are "bernoulli", "multi- nomial" or "rank" corresponing to the distributions of the observed variables.
obs	an array with dimensions (Total,J,max(Rj), max(Nijr)) corresponding to the observed data. For Bernoulli random variables, the data consist of 0/1's. For multinomial or rank data the data consist of integers 0,1,,(Vj[j]-1).

#### Details

The function returns an object of mixedMemModelVI class. This object contains dimensions of the model, the observed data, and the model parameters. Once a mixedMemModelVI object is created, the specified model can be fit for the data using the mmVarFit function. If the inputs are inconsistent (ie if dimensions do not match, or if observations and distribution types are not compatible, mixedMemModelVI will throw an error. For additional details on usage, and model assumptions, see the corresponding vignette "Fitting Mixed Membership Models Using mixedMem". Supported data types include Bernoulli, Multinomial, and Rank (Plackett-Luce). Note that the variational methods of mixedMem do not support the "Extended GoM" model which can be fit through the provided MCMC methods.

#### Value

returns an object of class mixedMemModelVI

## Examples

```
set.seed(123)
Total <- 50 # 50 Individuals
J <- 3 # 3 different variables
# distributions of each variable
dist <- c("multinomial", "bernoulli", "rank")
# 100 repeated measures of the multinomial, 5 repeated measures of the
# Bernoulli, 1 repeated measure of the rank
Rj <- c(100, 5, 1)</pre>
```

```
K <- 4 # 4 sub-populations</pre>
alpha <- rep(.5, K) #hyperparameter for dirichlet distribution
# Number of categories/alternatives for each variable. For the Bernoulli, Vj = 1
Vj <- c(10, 1, 4)
theta <- array(0, dim = c(J, K, max(Vj)))</pre>
# Parameters governing multinomial
theta[1,,] <- gtools::rdirichlet(K, rep(.3, Vj[1]))</pre>
# parameters governing Bernoulli
theta[2,,] <- cbind(rbeta(K, 1,1), matrix(0, nrow = K, ncol = Vj[1]-1))
theta[3,,] <- cbind(gtools::rdirichlet(K, rep(.3, Vj[3])),</pre>
matrix(0, nrow = K, ncol = Vj[1]-Vj[3]))
# Items selected for each observation. For Multinomial and Bernoulli, this is always 1
# For rank data, this will be the number of alternatives ranked
Nijr = array(0, dim = c(Total, J, max(Rj)))
Nijr[,1,c(1:Rj[1])] = 1 # N_ijr is 1 for multinomial variables
Nijr[,2,c(1:Rj[2])] = 1 # N_ijr is 1 for Bernoulli variables
Nijr[,3,c(1:Rj[3])] = sample.int(Vj[3], size = Total, replace = TRUE)
# generate random sample of observations
sampleMixedMem <- rmixedMem(Total, J, Rj, Nijr, K, Vj,</pre>
dist, theta, alpha)
## Initialize a mixedMemModel object
test_model <- mixedMemModel(Total = Total, J = J,Rj = Rj,</pre>
Nijr= Nijr, K = K, Vj = Vj,dist = dist, obs = sampleMixedMem$obs,
 alpha = alpha, theta = theta)
# Look at Summary of the initialized model
summary(test_model)
# Plot the current values for theta
plot(test_model)
```

mmMCMCFit

Fit Mixed Membership models using a Metropolis Hastings within Gibbs MCMC sampler

#### Description

Takes samples form the posterior distribution of a mixed membership model using a Metropolis-Hastings within Gibbs sampler.

#### Usage

```
mmMCMCFit(model, burnIn = 20000, samples = 1000, thin = 10, print = 100,
fileNames = c("theta.csv", "alpha.csv", "ksi.csv", "lambda.csv", "z.csv",
"p.csv", "rho.csv"), newFiles = 1, omega = 100, eta = 1,
whichWrite = c(1, 1, 1, 0, 0, 1, 0))
```

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## mmVarInfFit

#### Arguments

model	a mixedMemModelMCMC object created by the mixedMemModelMCMC constructor
burnIn	non-negative integer indicating the number of burn in samples before recording the first sample
samples	positive integer indicating the number of samples to record
thin	positive integer indicating how to thin the samples
print	positive integer indicating how often to print an update to the R console
fileNames	list of files locations to write samples. Should be vector of strings with length 5 (7 if using the extended mixed membership model) corresponding to: Theta, Alpha_0, Ksi, Lambda, Z, (P, rho).
newFiles	0 if samples should be appended to existing files; 1 if samples should overwrite any existing files
omega	tuning parameter for MH step for alpha.
eta	tuning parameter for MH step for ksi
whichWrite	which parameters to write to disk. Writing the individual parameters can signif- icantly increase computational time when the number of individuals is large
extended	boolean whether to estimate the extended model or not

#### Details

mmMCMCFit draws samples from the posterior distribution of a mixed membership model given a set of observed data. The sampler takes Metropolis Hastings steps to sample the  $\alpha_0$  and  $\xi$  parameters and samples the remaining  $\theta$ ,  $\lambda_i$  and Z parameters with a Gibbs sampler.

#### See Also

mixedMemModelMCMC

mmVarInfFit

Fit Mixed Membership models using variational EM

#### Description

mmVarInfFit is one of two primary computational function of the mixedMem package. The function fits parameters  $\phi$  and  $\delta$  for the variational distribution of latent variables as well as psuedo-MLE estimates for the population parameters  $\alpha$  and  $\theta$ . See documentation in the package vignette, "Fitting Mixed Membership Models Using mixedMem" for a more detailed description of the variables and notation in a mixed membership model.

## Usage

```
mmVarInfFit(model, printStatus = 1, printMod = 1, stepType = 3,
maxTotalIter = 500, maxEIter = 1000, maxAlphaIter = 200,
maxThetaIter = 1000, maxLSIter = 400, elboTol = 1e-06,
alphaTol = 1e-06, thetaTol = 1e-10, aNaught = 1, tau = 0.899,
bMax = 3, bNaught = 1000, bMult = 1000, vCutoff = 13,
holdConst = c(-1))
```

## Arguments

model	a mixedMemModelVarInf object created by the mixedMemModelVarInf con- structor.
printStatus	an integer 0 or 1. When printStatus is 1 mmVarInfFit will print status up- dates, when printStatus is 0 mmVarInfFit will not print status updates.
printMod	a positive integer which specifies how often to print status updates. The status will be printed at each step which is a multiple of printMod. The default value is 1.
stepType	an integer from 0-3 which specifies what steps to carry out in estimation. 0 per- forms a single E-Step; this can be used to find the held out ELBO. 1 performs iterates between E-steps and M-steps for estimating theta but keeps alpha con- stant. 2 iterates between E-steps and M-steps for estimating alpha, but keeps theta constant. 3 completes full E and M steps. The default is 3.
maxTotalIter	the maximum total steps before termination. A full E and M step together count as 1 step. If this maximum is ever achieved, a warning message will be printed at convergence. The default is 500.
maxEIter	the maximum iterations for each E-Step. If this maximum is ever achieved, a warning message will be printed at convergence. The default is 1000.
maxAlphaIter	the maximum iterations when fitting alpha. If this maximum is ever achieved, a warning message will be printed at convergence. The default is 200.
maxThetaIter	the maximum iterations when fitting theta. If this maximum is ever achieved, a warning message will be printed at convergence. The default is 1000.
maxLSIter	the maximum backtracking iterations in the line search for updating alpha and theta for rank data.
elboTol	the convergence criteria for the EM Algorithim. When the relative increase in the ELBO is less than the convergence critiera, the algorithm converges. The default is 400.
alphaTol	the convergence criteria for updates to alpha. When the relative increase in the ELBO is less than the convergence critiera, the update to alpha converges. The defualt is 1e-6.
thetaTol	the convergence criteria for updates to theta. When the relative increase in the ELBO is less than the convergence critiera, the update to theta converges. The default is 1e-10.
aNaught	the first step size in the backtracking line search used to update alpha and theta for rank data. The default is 1.
tau	the backtracking factor in the backtracking line search used to update alpha and theta for rank data. The default is .899.
bMax	the number of times the penalization factor is increased in the interior point method for fitting theta for rank data. The default is 3.
bNaught	the initial penalization factor in the interior point method for fitting theta for rank data. bNaught must be positive and the default value is 1000.
bMult	a positive number by which bNaught is multiplied by in each iteration of the interior point method for fitting theta for rank data. The default is 1000.

vCutoff	a positive integer cutoff for Vj at which a gradient ascent method is used instead of the Newton Raphson interior point method. This is used to avoid inverting a large matrix. The default is 13.
holdConst	a vector of integers specifying groups to be held fixed during the estimation procedure. The estimation algorithm will hold the theta parameters of these specific groups constant, but update all other parameters. The group numbers range from 0 to K - 1. To estimate all groups, use the default value of $c(-1)$ .

## Details

mmVarInfFit selects psuedo-MLE estimates for  $\alpha$  and  $\theta$  and approximates the posterior distribution for the latent variables through a mean field variational approach. The variational lower bound on the log-likelihood at the data given model parameters is given by Jensen's inequality:

$$E_Q \log[p(X, Z, \Lambda)] - E_Q \log[Q(Z, \Lambda | \phi, \delta)] \le \log P(obs | \alpha, \theta) \text{ where}$$

 $Q = \prod_{i} [Dirichlet(\lambda_{i} | \phi_{i}) \prod_{j}^{J} \prod_{r}^{\kappa_{j}} \prod_{n}^{N_{i,j,r}} Multinomial(Z_{i,j,r,n} | \delta_{i,j,r,n})]$ 

The left hand side of the above equation is often referred to as the Evidence Lower Bound (ELBO). The global parameters  $\alpha$  and  $\theta$  are selected to maximize this bound as a psuedo-MLE procedure. In addition, it can be shown that maximizing the ELBO with respect to the variational parameters  $\phi$  and  $\delta$  is equivalent to minimizing the KL divergence between the tractable variational distribution and the true posterior.

The method uses a variational EM approach. The E-step considers the global parameters  $\alpha$  and  $\theta$  fixed and picks appropriate variational parameters  $\phi$  and  $\delta$  to minimize the KL divergence between the true posterior and the variational distribution (or maximize the ELBO). The M-step considers the variational parameters fixed and global parameters  $\theta$  and  $\alpha$  are selected which maximize the lower bound on the log-likelihood (ELBO).

#### Value

mmVarInfFit returns a mixedMemModelVarInf object containing updated variational parameters and global parameters.

#### References

Beal, Matthew James. Variational algorithms for approximate Bayesian inference. Diss. University of London, 2003.

#### See Also

mixedMemModel

#### Examples

## The following example generates multivariate observations (both variables are multinomial)
## from a mixed membership model. The observed data is then used to fit a
## mixed membership model using mmVarFit

## Generate Data Total <- 30 #30 Individuals

```
J <- 2 # 2 variables
dist <- rep("multinomial",J) # both variables are multinomial</pre>
Rj <- rep(100,J) # 100 repititions for each variable
# Nijr will always be 1 for multinomials and bernoulli's
Nijr <- array(1, dim = c(Total, J, max(Rj)))</pre>
K <- 4 # 4 sub-populations
alpha <- rep(.5, K) # hyperparameter for dirichlet distribution
Vj <- rep(5, J) # each multinomial has 5 categories
theta <- array(0, dim = c(J, K, max(Vj)))
theta[1,,] <- gtools::rdirichlet(K, rep(.3, 5))</pre>
theta[2,,] <- gtools::rdirichlet(K, rep(.3, 5))</pre>
obs <- rmixedMem(Total, J, Rj, Nijr, K, Vj, dist, theta, alpha)$obs
## Initialize a mixedMemModel object
test_model <- mixedMemModel(Total = Total, J = J,Rj = Rj, Nijr= Nijr,</pre>
K = K, Vj = Vj,dist = dist, obs = obs,
  alpha = alpha, theta = theta+0)
## Fit the mixed membership model
out <-mmVarInfFit(test_model)</pre>
```

permuteLabels Mixed Membership Post-Processing

## Description

Mixed Membership models are invariant to permutations of the sub-population labels; swapping the names of each sub-population yields an equivalent model. The ordering of the labels in a fitted model is dependent on the initialization points of the variational EM algorithm. The permuteLabels function returns a mixedMemModel object where the labels (for  $\theta$ ,  $\phi$ ,  $\delta$  and  $\alpha$ ) have been permuted according a given permutation of the integers 1 through K. The findLabels function can be used to find a permutation of the labels which most closely matches another fitted model.

#### Usage

```
permuteLabels(model, perm)
```

#### Arguments

model	a fitted mixedMemModel object which will be relabeled.
perm	a vector of length K with integers 1:K. This is the permutation by which to relabel the mixedMemModel object such that group i in the returned mixedMemModel object corresponds to group perm[i] from the input mixedMemModel object.

#### Value

permuteLabels returns a mixedMemModel object such that group i in the returned mixedMemModel object corresponds to group perm[i] from the input mixedMemModel object

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## See Also

findLabels

plot.mixedMemModelMCMC

Plot a Mixed Membership Model

## Description

Generic S3 function to produce visual representation of a mixedMemModelMCMC object. This function calls either the vizTheta or the vizMem function.

## Usage

## S3 method for class 'mixedMemModelMCMC'
plot(x, type = "theta", compare = NULL,
 main = NULL, varNames = NULL, groupNames = NULL, nrow = NULL,
 ncol = NULL, indices = NULL, fitNames = NULL, ...)

#### Arguments

х	the mixedMemModel object to be plotted.
type	a string which indicates which estimated parameters to plot; valid options are "theta" or "membership". vizTheta is called when the type is "theta" and vizMem is called when the type is "membership".
compare	an array or matrix for comparison. When type = "theta", compare should be an array the same size as x\$theta. When type = "membership", compare should be a matrix the same size as x\$phi.
main	the main figure title.
varNames	a vector of strings corresponding to names for each variable if plot type is theta.
groupNames	a vector of strings corresponding to labels for each sub-population.
nrow	the number of rows for the grid of plots.
ncol	the number of columns for the grid of plots. If plot type is "theta", this must be K, if plot type is "membership", this must be a positive integer.
indices	a vector of integers. If the plot type is "membership", this indicates which in- dividuals to plot. When plot type is "theta", this indicates which variables to plot.
fitNames	a vector of strings corresponding to labels for each fit.
	additional parameters to be passed.

#### See Also

mixedMemModelMCMC, vizTheta, vizMem

plot.mixedMemModelVarInf

Plot a Mixed Membership Model

## Description

Generic S3 function to produce visual representation of a mixedMemModelVarInf object. This function calls either the vizTheta or the vizMem function.

## Usage

```
## S3 method for class 'mixedMemModelVarInf'
plot(x, type = "theta", compare = NULL,
   main = NULL, varNames = NULL, groupNames = NULL, nrow = NULL,
   ncol = NULL, indices = NULL, fitNames = NULL, ...)
```

## Arguments

х	the mixedMemModelVarInf object to be plotted.
type	a string which indicates which estimated parameters to plot; valid options are "theta" or "membership". vizTheta is called when the type is "theta" and vizMem is called when the type is "membership".
compare	an array or matrix for comparison. When type = "theta", compare should be an array the same size as x\$theta. When type = "membership", compare should be a matrix the same size as x\$phi.
main	the main figure title.
varNames	a vector of strings corresponding to names for each variable if plot type is theta.
groupNames	a vector of strings corresponding to labels for each sub-population.
nrow	the number of rows for the grid of plots.
ncol	the number of columns for the grid of plots. If plot type is "theta", this must be K, if plot type is "membership", this must be a positive integer.
indices	a vector of integers. If the plot type is "membership", this indicates which in- dividuals to plot. When plot type is "theta", this indicates which variables to plot.
fitNames	a vector of strings corresponding to labels for each fit.
	additional parameters to be passed.

#### See Also

mixedMemModelVI, vizTheta, vizMem

## Description

Mixed Membership Post-Processing for MCMC method

plotPosterior

## Usage

```
plotPosterior(model, fileName, parameter, addToExisting = F,
    plotType = "trace", j = 1, k = 1, v = 1, s = 1, ...)
```

## Arguments

model	the fitted mixedMemModelMCMC object.
fileName	a string containing the file paths for the MCMC output
parameter	which parameter to plot
addToExisting	whether to plot on existing plot or new plot
j	the jth element to plot
k	the kth element to plot
v	the vth element to plot
S	the sth element to plot
	additional commands passed to plotting function
type	histogram or trace plot

Simulate Data from a discrete mixed membership model

## Description

Simulate Data from a discrete mixed membership model

#### Usage

```
rmixedMem(Total, J, Rj = rep(1, J), Nijr = array(1, dim = c(Total, J,
max(Rj))), K, Vj, dist, theta, alpha, lambda = NULL)
```

rmixedMem

#### Arguments

Total	the number of individuals in the sample.
J	the number of variables observed on each individual.
Rj	a vector of positive integers of length J specifying the number of repeated mea- surements for each variable.
Nijr	an array of dimension (Total, J, max(Rj)) indicating the number of ranking levels for each replication. For multinomial and Bernoulli variables, Nijr[i,j,r] = 1. For rank variables, Nijr[i,j,r] indicates the number of items ranked for each individual.
К	the number of latent sub-populations.
Vj	a vector of length J specifying the number of possible categories for each variable. For a Bernoulli variable $Vj[j] = 1$ . For a multinomial or rank variable, $Vj[j]$ is the number of possible categories/items.
dist	a vector of strings of length J specifying variable types. Options are "bernoulli", "multinomial" or "rank" corresponing to the distributions of the observed vari- ables.
theta	an 3 way array of dimensions $(J,K,max(Vj))$ which governs the variable distributions. Parameter theta[j,k,] governs the distirbution of responses on variable j for an inidvidually completely in sub-population k. If the number of items/categories differs across variables, any unusued portions of theta should be set to 0. @param lambda an optional matrix of dimensions (Total, K) containing the membership scores for each individual. If the lambda argument is not specified, the group membership scores will be automatically sampled from a Dirichlet(alpha)
alpha	a positive K-length vector which is the parameter for the Dirichlet distribution of membership scores.

## Details

rmixedMem simulates data from a mixed membership model given the specified parameters and dimensions. The function returns a random sample of observations obs, context indicators Z, and group membership scores lambda.

## Value

rmixedMem returns a list containing a three items: A matrix of group memberships scores lambda, an array of context indicators Z and an array of observations obs.

summary.mixedMemModelMCMC

Summary of a Mixed Membership Model

## Description

Generic S3 summary function for mixedMemModelMCMC class.

## Usage

```
## S3 method for class 'mixedMemModelMCMC'
summary(object, ...)
```

## Arguments

object	$\label{eq:constraint} the \verb"mixedMemModelMCMC" object to be summarized$
	additional parameters

## Details

summary provides a summary of the given mixedMemModelMCMC object. The function prints the ELBO, the dimensions of the model and each variable type.

## See Also

mixedMemModelMCMC

summary.mixedMemModelVarInf

Summary of a Mixed Membership Model

## Description

Generic S3 summary function for mixedMemModelVarInf class.

#### Usage

```
## S3 method for class 'mixedMemModelVarInf'
summary(object, ...)
```

## Arguments

object	the mixedMemModelVarInf object to be summarized
	additional parameters

## Details

summary provides a summary of the given mixedMemModelVarInf object. The function prints the ELBO, the dimensions of the model and each variable type.

## See Also

mixedMemModelVI

theta.table

## Description

Print the theta estimates for each sub-population to the R console in a more aesthetically pleasing manner

## Usage

```
theta.table(model, digits = 3, top.level = "group")
```

## Arguments

model

the mixedMemModel who's theta will be printed.

## See Also

mixedMemModel, vizTheta

vizMem

Mixed Membership Visualization

#### Description

vizMem plots estimates for the group membership scores of each individual. This is the function called by the mixedMemModel class generic plot function.

#### Usage

```
vizMem(model, compare = NULL, main = "Estimated Membership", nrow = NULL,
ncol = NULL, indices = NULL, groupNames = NULL, fitNames = NULL)
```

## Arguments

model	the mixedMemModelVI or mixedMemModelMCMC object that will be plotted.
compare	a matrix of dimension (Total, K) which contains parameters to compare against the fitted model.
main	the main figure title.
nrow	the number of rows in each plot.
ncol	the number of columns in each plot.
indices	the specific individuals which will be shown in the plot. If the argument is left blank, all individuals will be plotted. If the number of individuals to be plotted is larger than nrow * ncol then multiple plots will be produced.
groupNames	a vector specifying labels for each sub-population.
fitNames	a vector of length 2 containing strings which correspond to the names of the models (fitted and comparison).

#### vizTheta

#### Details

For a mixedMemModelVI object, the estimates plotted are the normalized  $\phi$ , which are the posterior means from the variational distribution. For a mixedMemModelMCMC object, the estimates plotted are the point estimates for  $\lambda_i$ . The estimated group membership scores are shown in black, and the estimates from a comparison model (if available) are shown in red. Each plot represents an individual.

vizTheta

Mixed Membership Visualization

#### Description

vizTheta plots  $\theta$ , the parameters which govern the sub-population distributions of variables in a mixed membership model. The parameter  $\theta_{j,k}$  specifies the distribution of variable j for complete members of sub-population k. The estimated parameters from the given model are shown in black in each plot; the parameters from a comparison model (if available) are shown in red. Each row of plots represents a single variable, and each column of the plots represents a sub-population.

#### Usage

```
vizTheta(model, compare = NULL, main = "Estimated Theta", varNames = NULL,
groupNames = NULL, nrow = NULL, fitNames = NULL, indices = NULL)
```

#### Arguments

model	the mixedMemModelMCMC or mixedMemModelVI object that will be plotted.
compare	an array of the same dimensions as model\$theta which contains values to com- pare against the fitted value.
main	the main figure title.
varNames	a vector of strings specifying labels for each variable.
groupNames	a vector of strings specifying labels for each sub-population.
nrow	the number of rows in each plot. If the argument is not specified, all variables will appear in one plot.
fitNames	the names of the models plotted.
indices	a vector which indicates specific variables to plot. If the argument is not spec- ified, all variables will be plotted. If the number of variables to plot is greater than nrow, then multiple plots will be produced.

#### Details

This is the function called by the plot generic function for mixedMemModel objects.

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